Multivariate Stochastic Approximation to Tune Neural Network Hyperparameters for Critical Infrastructure Communication Device Identification

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Abstract
The e-government includes Wireless Personal Area Network (WPAN) enabled internet-to-government pathways. Of interest herein is Z-Wave, an insecure, low-power/cost WPAN technology increasingly used in critical infrastructure. Radio Frequency (RF) Fingerprinting can augment WPAN security by a biometric-like process that computes statistical features from signal responses to 1) develop an authorized device library, 2) develop classifier models and 3) vet claimed identities. For classification, the neural network-based Generalized Relevance Learning Vector Quantization-Improved (GRLVQI) classifier is employed. GRLVQI has shown high fidelity in classifying Z-Wave RF Fingerprints; however, GRLVQI has multiple hyperparameters. Prior work optimized GRLVQI via a full factorial experimental design. Herein, optimizing GRLVQI via stochastic approximation, which operates by iterative searching for optimality, is of interest to provide an unconstrained optimization approach to avoid limitations found in full factorial experimental designs. The results provide an improvement in GRLVQI operation and accuracy. The methodology is further generalizable to other problems and algorithms.

1. Introduction

The e-government provides for the efficient information dissemination via electronic means and the necessary information and communication technologies (ICTs) for information dissemination within and around the government [1]. Due to the sensitivity of information, securing e-government networks is a primary concern [2]. However, adequately securing e-government networks, servers, firewalls and content is an issue with known deficiencies [2].

Wireless Personal Area Network (WPAN) devices are commonly low-cost and low-power devices which enable mesh networks comprised of smart internet of things (IoT) devices [3]. Z-Wave devices are among the IoT enabling WPAN devices which support e-government [4]. Increasingly, such devices are found in e-government and Critical Infrastructure (CI) applications such as hospital [5] and electrical smart grid [6].

Security issues exist with Z-Wave, and other WPAN devices, due to 1) government-to-internet pathways, 2) the tendency for e-government connections to Critical Infrastructure (CI) control technologies, e.g. [7], and 3) since one compromised device can threaten the security of the entire network [8]. These issues are compounded by inherent vulnerabilities in WPAN technologies, see [9] [10]. For these reasons, enabling robust security by improving the ability to determine Z-Wave device identities, e.g. after they have claimed a bit-level identify (such as MAC address), is of interest.

To vet the identity of Z-Wave WPAN devices, the standard three step process (library building, classifier model development, and verification), as used in biometrics [11], is followed. However, to characterize communication devices, one logically compares predefined signal characteristics, such as preambles, between devices operating on the same standard. For this purpose, Radio Frequency (RF) fingerprinting is used whereby the communication signal of interest is examined, divided into bins, and statistical features are computed for each bin [12].

To discriminate between devices using RF fingerprint features, machine learning (ML) methods are employed. Two ML methods have generally been employed: Multiple Discriminant Analysis (MDA) and the Generalized Relevance Learning Vector Quantization-Improved (GRLVQI) classifier. MDA is a linear ML algorithm whereas GRLVQI is a nonlinear Artificial Neural Network (ANN) algorithm. Generally, for Z-Wave, GRLVQI outperforms MDA in classification accuracy [13]. However, GRLVQI has multiple algorithmic settings, called hyperparameters, which influence the way in which the classifier is trained. Little has been published in GRLVQI, or ANN, literature on these hyperparameters beyond
vague guidelines for very specific applications [14] [15].

Prior work, c.f. [13], examined full factorial GRLVQI algorithm optimization relative to Z-Wave device identification for its five hyperparameters. However, the results and approach of [13] were not ideal since they: 1) were highly tailored to the example Z-Wave dataset and thus possibly not applicable to other WPAN device signals, 2) involved exploring only a small region of the design space and utilized subject matter expertise to find appropriate high (+) and low (−) settings, and 3) involved only a single replication and thus ignored the randomness existing in any ANN algorithm, including GRLVQI, result.

Efficiently determining optimal hyperparameters is thus of interest. More efficient alternatives to the approach of [13] include 1) considering an alternative experimental designs, e.g. [16] [17], and 2) stochastic estimation, e.g. [18]. Although various experimental design approaches have been used to find optimal hyperparameter settings, see [19], these do not avoid the limitations in specifying the high and low settings to examine. Stochastic approximation begins with initial hyperparameter settings and proceeds to search throughout the space to find optimal settings. Thus stochastic approximation is of interest since it does not artificially restrict the search space.

This work presents a framework for general algorithm optimization via stochastic approximation for sequential design. In doing so, this extends the initial work of [18] by allowing GRLVQI to find optimal settings in an iterative fashion for its four continuous hyperparameters: gradient descent learning rate (ε), relevance learning rate (ξ), conscience rate 1 (γ), and conscience rate 2 (β). Additionally, the work of [13] is extended by creating a more efficient approach to optimizing GRLVQI settings and by creating a more robust approach to GRLVQI optimization by averaging replication results.

2. WPAN Devices and E-Government Concerns

While much of the ICTs used in e-government applications involve access to information [20], increasingly the e-government includes other communication technologies such as WPAN devices [3] [21] and Supervisory Control and Data Acquisition (SCADA) [22] systems. SCADA systems generally connect to infrastructure, including CI, while WPAN devices serve as a backbone for IoT connectivity where devices ranging from refrigerators to Heating, Ventilation and Air Conditioning (HVAC) [23]. While these systems can be separate, and more secure, e-government pathways can exist through systems being connected at various points; thus there generally exist a link between these networks and the internet [24] [25].

2.1. Z-Wave Devices

Z-Wave devices are a wireless communication devices are small, low-cost hardware devices that are advantageous for WPANs because they support many network topologies, is simpler to work with than ZigBee [26]. However, Z-Wave is generally considered as less secure than competing WPAN technologies given 1) originally lacked built in encryption [27] and 2) the proprietary nature of the standard making it difficult for third parties to provide enhancements [28].

Vendors are largely responsible for integrating Z-Wave capabilities into their system. However, to produce a Z-Wave device, vendors must coordinate with Sigma Designs and sign a Non-Disclosure Agreement (NDA) to gain access to the proprietary details of the Z-Wave standard. Once an NDA is in place, hardware and software to develop Z-Wave devices are provide by Sigma Designs [10]. While Sigma Designs will provide examples to vendors who sign an NDA, without a signed NDA specific characteristics of the protocol are unknown [10]. The protocol describes general physical layer (PHY) and medium access layer characteristics, but the routing and application layer specifications are protected by the NDA enforced by Sigma Designs [10]. Thus one is confronted with a digital forensics, c.f. [29] [30], problem in analyzing the Z-Wave standard without an NDA and being bound by its restrictions.

![Z-Wave device protocol characteristics](image)

Figure 1. Z-Wave device protocol characteristics [27] [28] [31].

What is known about Z-Wave is that it follows the ITU-T G.9959 protocol [32], which is a similar ISO architecture to ZigBee and TCP/IP, as seen in Figure 1. General Z-Wave signal characteristics are known and presented in Table 1. Z-Wave is also known to have a predefined preamble and Start of Frame (SoF) [31], which is conceptualized in the PHY packet structure seen in Figure 2. Z-Wave also includes a payload-based home identification (32-bits) and source identification (8-bits) [28]. Due to their proprietary
nature, further knowledge of Z-Wave signal characteristics is limited and thus digital forensic analysis of Z-Wave devices remains an emerging area of interest [10].

**Table 1. General Z-Wave Device Characteristics**

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Z-Wave</th>
</tr>
</thead>
<tbody>
<tr>
<td>Device</td>
<td>Z-Wave</td>
</tr>
<tr>
<td>Standard</td>
<td>Proprietary</td>
</tr>
<tr>
<td>Frequency</td>
<td>906 MHz</td>
</tr>
<tr>
<td>Bit Rate</td>
<td>40 Kbits/s</td>
</tr>
<tr>
<td>Security</td>
<td>None (200 and 300 series models)</td>
</tr>
<tr>
<td></td>
<td>AES 128 (400 series models)</td>
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<tr>
<td>Latency</td>
<td>~1000 ms</td>
</tr>
<tr>
<td>Range</td>
<td>30 - 100 m</td>
</tr>
<tr>
<td>Message Size (Bytes)</td>
<td>64 (max)</td>
</tr>
<tr>
<td>Topology</td>
<td>Star, cluster, mesh</td>
</tr>
</tbody>
</table>

**Figure 2. Z-Wave device signal characteristics [27] [28] [31].**

3. RF Fingerprinting

RF Fingerprinting, as conceptualized in Figure 3 via the RF-DNA (Distinct Native Attributes) fingerprinting process of [12], is a systematic process of collecting communication signals. RF fingerprinting involves selecting a Region of Interest (ROI) to extract, then digital filtering, computation of the instantaneous amplitude, frequency and phase, fingerprint generation, and finally classifier model development and verification testing [12]. To simulate degraded and distance collections and environmental conditions, independent like-filtered Additive White Gaussian Noise (AWGN) is added to collected signals [12].

When used effectively, RF fingerprinting provides biometric-like security of communication devices whereby unique fingerprint features are computed for a communication signal’s ROI. Fingerprint features of variance, skewness and kurtosis are used for this task [12], which is similar to the use of mathematical moments for identification problems [33]. Standard predefined ROIs, e.g. preambles which have a specified sequence of 1s and 0s, are selected for RF fingerprinting and then RF fingerprint features are computed for this ROI. Due to production variations inherent in integrated circuit manufacturing, minute differences between devices at a serial number level are resolvable through RF fingerprinting.

3.1 Z-Wave Signal Collection

The work herein considered the Z-Wave dataset used previously in [13] [34]. This dataset considered three devices, \( N_D = 3 \), which were Aeon Labs’ Aeotec Z-Stick S2 transmitters. As discussed in Section 2.2, characteristics of the preamble response (the first 8.3 ms of Z-Wave bursts) are known for Z-Wave and this was considered as the ROI for RF fingerprinting.

![Figure 3. Conceptualization of Z-Wave signal collection within the RF fingerprinting generation and exploitation process of [12]](image-url)
Responses were collected for each device at a sample frequency of $f_s = 2 \text{ Mbps}$ with burst detection via an amplitude-based leading edge detector with a -6 dB threshold [34]. The resultant data was collected with a Signal-to-Noise Ratio (SNR) at $SNR_C = 24.0 \text{ dB}$ [34]. AWGN was applied to achieve operating conditions of $SNR \in [0 \text{ to } 24.0] \text{ dB}$ in 2 dB increments [34] [12]. Since 3 devices were considered, all devices were considered as serving in “authorized” roles. Thus, this research does not consider identity impersonation attacks by “rogue” devices.

### 3.2. RF-DNA Fingerprint Generation

Once burst signals were collected, RF fingerprints were generated from the preamble ROI, as in the RF-DNA [12] [34]. RF fingerprints were computed by 1) dividing each response into $N_R$ contiguous equal length bins, 2) calculating $N_F$ features within each bin and across the entire response ($N_F + 1$ total bins), and 3) computing regional fingerprint vectors [34], [12]. RF regional fingerprint vectors were organized as,

$$F_{RI} = [\sigma_{RI}^2, \gamma_{RI}, \kappa_{RI}]_{1 \times 3},$$  

where $i = 1,2, ..., N_R + 1$, for the $N_F = 3$ RF fingerprint features (statistics) of variance ($\sigma^2$), skewness ($\gamma$), and kurtosis ($\kappa$) [34], [12]. This process is conceptualized in Figure 4.

- **Figure 4.** Conceptualization of Z-Wave RF fingerprint computation

A fingerprint vector for each of the $N_C$ characteristics is formed from (1) as,

$$F^C = \left[ F_{R_1} \ F_{R_2} \cdots \ F_{R(N_R+1)} \right]_{1 \times N_F(N_R+1)} \ .$$  

which are concatenated to form the final fingerprint vector:

$$F = \left[ F^a : F^\phi : F^f \right]_{1 \times N_F(N_R+1) \times N_C} \ .$$  

For Z-Wave device discrimination assessments, and consistent with [34], $N_R = 20$ subregions spanning the ROI were considered within $N_C = 3$ Z-Wave instantaneous time domain responses of amplitude ($a$), phase ($\phi$), and frequency ($f$). Thus, a total of $N_F = 189$ features are computed with $N_{TRN} = 115$ Training (TNG) and $N_{TST} = 115$ Testing (TST) observations per device. When considering the $N_C = 3$ devices, our dataset has a total of $N_{TRN} = 345$ and $N_{TST} = 345$, each with $N_F = 189$ features. To avoid the possibility of overfitting, the TNG and TST data was sequestered during model development.

### 3.3. Classifier Models

Various classifiers have been applied for discriminating between communication devices based on RF Fingerprints, as seen in [35]. However, MDA and GRLVQI are of interest herein due to their illustrated performance advantages in RF fingerprinting problems [13] [34].

#### 3.3.1. GRLVQI Classifier Model

The GRLVQI classifier employed herein is based on the work in [36], [35] and extends the Learning Vector Quantization (LVQ) approach of Kohonen [15]. LVQ algorithms are epistemologically self-organizing ANNs [37], and employ nearest neighbor approaches through the nearest prototype vector optimization process whereby the “nodes” or “prototype vectors” (PVs) of the ANN are iteratively moved to characterize the data [38]. In operation, LVQ algorithms train prototype vectors to a given class label by moving correctly classified PVs closer to a given class, incorrectly classified PVs are moved away from a given class. The additional letters in the GRLVQI acronym signify embellishments to the algorithm: $G$ (generalized): a sigmoidal cost function [39] [40], $R$ (relevance): relevance learning [41] [42], and $I$ (improved): improvements in PV update logic and operation [36] [43]. GRLVQI extends GRLVQ [42] with the conscience learning of DeSieno [44], improved PV update logic, and a frequency based maximum input update strategy [36].

Due to the embellishments, GRLVQI has five hyperparameters to consider when creating a model: 1) the gradient descent learning rate ($\epsilon$) which determines how fast the PVs move [15], 2) the relevance learning rate ($\xi$), which determines how quickly variables are penalized for being insignificant [41], [42], 3-4) conscience rate 1 ($\gamma$), and conscience rate 2 ($\beta$), which both determine how frequently individual PVs should be moved [36], [43] and 5) the number of prototype vectors ($N_N$) instantiated per...
class, which balances under and overfitting. Beyond rough heuristics, c.f. [14] [42], no “hard and fast” rules exist to determine GRLVQI parameters [36].

3.3.2. Multiple Discriminant Analysis. MDA is a linear approach to classification which is a multi-class extension of Fisher’s two class linear classifier [35]. MDA considers input fingerprint matrix \( F \) and \( N_C \) classes and involves an eigenvector-based projection of the data relative to a ratio of between-group to within-group sum-of-squares, the Fisher criterion [45]. Since MDA is intuitive, computationally inexpensive and has shown significant performance advantages over GRLVQI for many RF-DNA Fingerprinting problems, e.g. ZigBee [34], it is included to provide a baseline performance reference, consistent with [35]. Additionally, MDA classifier results are not susceptible to random variations due to sampling since this provides a direct projection of the data.

3.4. Quantifying Algorithm Performance

Consistent with [13], both classification and verification accuracy is considered. Classification accuracy is considered by developing classifier models for each SNR operating point and then evaluating performance for against both the TNG and TST datasets in a traditional confusion matrix approach for “one vs. many” scenarios as in [12]. Verification accuracy is considered in a “one vs one” scenario for a developed classifier model whereby a communication device claims an identity, authorized or rogue/unauthorized, and the communication device’s signal is evaluated using the classifier model and the associated probability mass function [46].

3.4.1. Classification Accuracy. Classification performance is evaluated by examining a plot of average percent correct classification (%C) versus SNR [13]. Consistent with [13], both a gain measure and an area under the classification curve approach can be used. Here, gain is defined as the reduction in required SNR, expressed in dB, for two methods to achieve the same %C, generally an arbitrary performance benchmark of %C = 90% accuracy [13] [47]. However, gain only considers one part of the %C vs. SNR curve; the Relative Accuracy Percentage (RAP) was introduced in [13] to provide for classifier assessment over the entire curve by 1) computing the Area Under Classification Curve (AUCC) values for each method via a trapezoidal approximation, and 2) computing the RAP of a given method’s AUCC relative to the baseline AUCC\(_{base}\) method.

As discussed in [13], gain values, \( G_{SNR} \), are interpreted as follows:

1) \( G_{SNR} < 0.0 \) (negative), a given method achieves the same %C as the baseline at a higher SNR, i.e. the method underperforms the baseline method.
2) \( G_{SNR} = 0.0 \), a given method achieves the same %C as the baseline at the same SNR
3) \( G_{SNR} > 0.0 \) (positive), a given method achieves the same %C as the baseline at a lower SNR, i.e. the method outperforms the baseline method.

As developed in [13], RAP is interpreted as:

1) \( RAP < 1.0 \), a given method achieves overall lower %C than the baseline
2) \( RAP = 1.0 \), a given method achieves overall %C comparable to the baseline
3) \( RAP > 1.0 \), a given method exceeds overall baseline %C performance.

3.4.2. Verification Accuracy. Verification performance is evaluated using Receiver Operating Characteristic (ROC) curves at a specified SNR, typically at the lowest SNR a %C = 90% accuracy threshold is reached [13]. In operation, and as described in [47], [46], verification involves: 1) an -unknown device claiming bit level credentials (e.g., MAC address) which matching a specific authorized device, 2) extracting RF fingerprint features from the unknown device, and 3) comparing current RF fingerprints against the model for the claimed device, having the claimed identity. For authorized devices, ROC curves are plotted as True Verification Rate (TVR) versus False Reject Rate (FRR). To evaluate performance, two approaches are used [13]: 1) the percentage authorized (%Aut) at an arbitrary TVR ≥ 90% at FVR ≤ 10% threshold and 2) the mean area of the ROC curves (AUCM). The AUCM approach was developed in [13] since %Aut reflects coarse and dichotomous sampling and dichotomous, e.g. \( N_d = 3 \) devices %Aut ∈ [0, 33, 66, 100], and thus %Aut does not distinguish between relative performance differences between competing classifiers.

4. Multivariate Stochastic Approximation based Optimization of Hyperparameters

Consistent with general ANN operations, the performance of the GRLVQI classification algorithm after training is a random variable as the training data set is randomly selected. Thus, determining optimal hyperparameters for the GRLVQI requires an appropriate experimental design.

We use a sequential design strategy [48] which begins with an initial guess of the hyperparameter settings. Based on these settings, GRLVQI is trained and the results from this training determine a new set
of hyperparameters. This procedure is repeated until it converges on a particular set of hyperparameters. To update the hyperparameter values each iteration, we use the method of Kiefer and Wolfowitz [49], which is a stochastic approximation version of gradient descent optimization.

We present a minimal amount of the theory behind stochastic approximation to demystify the pseudocode for the optimization algorithm.

4.1. Stochastic Approximation Theory

For the Kiefer and Wolfowitz approach of our sequential design strategy, we will let \( h_{i,j} \) be the value of the \( j \)th of \( N \) continuous valued hyperparameter of the GLVQI at iteration \( j \) of the optimization procedure, and let \( h_j \) be vector of these hyperparameters. Let \( f(h_j) \) be the performance measure of interest of GRLVQI. Finally, let \( \{a_n\} \) and \( \{c_i\} \) be sequences such that

\[
\sum_{i=1}^{\infty} a_i = \infty, \\
\sum_{i=1}^{\infty} a_n c_n < \infty, \\
\sum_{i=1}^{\infty} c_i a_n^{-2} < \infty. 
\]

Using (5), let \( c_i^j = (0^{i-1}, c_i, 0^{N-i}) \) where \( 0^n \) is a vector of zeroes of size \( n \). The iteration function is given by

\[
\begin{bmatrix}
  h_{1,j+1} \\
  \vdots \\
  h_{n,j+1}
\end{bmatrix} = \frac{a_i}{2c_i} \begin{bmatrix}
  f(h_j + c_i^j) - f(h_j - c_i^j) \\
  \vdots \\
  f(h_j + c_n^j) - f(h_j - c_n^j)
\end{bmatrix}
\]

The algorithm terminates when the norm of the differences between \( f(h) \) of two consecutive iterations is small.

It should be noted that stochastic approximation finds locally optimal solutions, which are potentially significantly different from the globally optimal solutions. While it is never possible to be sure that we have arrived at the globally optimal solution with stochastic approximation, we can identify multiple locally optimal solutions and select the best by running the algorithm multiple times with different initial solutions (however, for this work, we have chosen to do only one run).

4.2. Sequential Design Algorithm

In operation, the process in Section 4.1 can be applied to a given algorithm by following a few steps. Specifically we employ the following algorithm to find the (locally) optimal hyperparameters of \( \epsilon, \xi, \gamma, \) and \( \beta \) for GRLVQI; however, this can be applied to many other algorithms.

The algorithm works as follows, with \( \tau \) being a termination criteria and \( \bar{f}_{N_{\text{rep}}}(h_i) \) representing the mean value of RAP values after training individual GRLVQI classifiers for \( N_{\text{rep}} \) replications. Also let \( |h_i - h_{i-1}| \) be the L1 norm of \( h_i \) and \( h_{i-1} \).

1. Set \( i = 1 \).
2. Specify initial hyperparameter values for \( \epsilon_1, \xi_1, \gamma_1, \) and \( \beta_1 \).
3. Let \( h_1 = (\epsilon_1, \xi_1, \gamma_1, \beta_1) \).
4. While \( |h_i - h_{i-1}| < \tau \) or \( i \geq 1 \)
   a. Set \( a_i = \frac{0.1}{i} \) and \( c_i = 0.001i^{-1/3} \).
   b. Set \( \text{RAP}_{u,1} = \bar{f}_{N_{\text{rep}}}(h_i + c_1^j) \), \( \text{RAP}_{l,1} = \bar{f}_{N_{\text{rep}}}(h_i - c_1^j) \), \( j = 1, \ldots, 4 \), and \( N_{\text{rep}} = 10 \).
   c. Set \( h_{i+1} = \frac{a_i}{2c_i} \begin{bmatrix}
    \text{RAP}_{u,1} - \text{RAP}_{l,1} \\
    \vdots \\
    \text{RAP}_{u,4} - \text{RAP}_{l,4}
\end{bmatrix} \)
   d. Set \( \text{RAP}_{i+1} = \bar{f}_{N_{\text{rep}}}(h_{i+1}) \).
   e. Set \( i = i + 1 \).
5. Return \( h_i \).

The termination criteria, \( \tau \), is used to comparing the norm of the difference between the current iteration hyperparameter values, \( h_i \), and its value from the last iteration, \( h_{i+1} \); thus when these results are sufficiently similar, the algorithm will stop. The initialization steps, \#1-3 initialize the decay terms, the iteration counter, \( i \), and the initial operating point of the algorithm. Step 4a specify how the decay terms are updated which monotonically decrease as the algorithm progresses. Step 4b runs the algorithm multiple times, each with a hyperparameter increased and decreased by \( c \); in this case we have four hyperparameters and GRLVQI was run twice for each setting (8 times total) and then the process was replicated 10 times to improve the estimate of GRLVQI performance with a given set of hyperparameters. Step 4c is in essence performing a gradient descent by examining the differences between the scores with \( c (N_{\text{cond}} = 2 \) conditions). and adjusting the hyperparameter values accordingly. Step 4d sets

\[1\] Suggested sequences are \( \{a_n\} = \frac{1}{n} \) and \( c_n = n^{-2} \)
the value of this iteration’s results and Step 4e increments the iteration counter. Step 5 returns the optimal setting values for GRLVQI.

5. Learning Vector Quantization Setting Optimization

Work in [13] aimed to find optimal LVQ settings by using a full factorial model with optimal settings found via both a spreadsheet search and a response surface method with constrained nonlinear optimization. However, two limitations exist with the approach of [13]:

1) The full factorial approach was limited by exploring only a constrained region of the possible design space.
2) Lack of sufficient replications to account for random variation.

5.1. Experimental Considerations

The Sequential Design strategy via Stochastic Approximation approach discussed in Section 4 was used to account for the first issue by allowing the $N_{hyp} = 4$ continuous hyperparameters $(\epsilon, \xi, \gamma, \beta)$ of GRLVQI to be optimized by consideration $\pm c$. Consistent with [35], $h_0 = (0.025, 0.005, 2.5, 3.5)$ was used.

To account for the second issue, $N_{rep} = 10$ replicates were considered for all steps in the process to account for random variation. Optimization was considered with respect to maximum possible RAP, from 100% $\%C$ for all explored SNR operating points. Optimization was performed with respect to the TNG set performance to avoid training on testing data.

In total, with $N_{hyp} \times N_{rep} \times N_{cond} = 80$ GRLVQI runs were computed for each iteration. The average RAP was computed for GRLVQI by hyperparameter. The stochastic approximation approach was allowed to run until the norm between latest iteration and last iteration was 0.01. This resulted in $N_{iter} = 28$ iterations being run, thus 2,240 total GRLVQI classifiers were developed.

5.2. Results

By evaluating the hyperparameter settings through each iteration, Figure 5, we can gather some indication of the path the stochastic approximation algorithm took where each subplot examines the respective rate versus iteration number. Figure 5a shows the learning rate progression shows a continual increase. Figure 5b shows the relevance rate progression which climbs fast and then oscillates around 0.02. Figure 5c and Figure 5d show the progression for the conscience learning rates, which quickly hit a general plateau.

Although the progression of the learning rate in Figure 5a shows a continual climb, this is being counteracted by the decaying property of $c$ in the algorithm. Additionally, we can examine the RAP values at each iteration (using a baseline of the maximum possible achievable performance of 100% $\%C$ at all SNR). Figure 6 shows the RAP values with error bars computed from the replicated runs. In Figure 6 we see that the algorithm climbs quickly from an initial RAP of approximately 0.63 and then levels off to an RAP of approximately 0.645. The error bars illustrate that this performance improvement is a significant improvement over the initial settings.

![Figure 5. Hyperparameter settings through 28 iterations](image)

![Figure 6. RAP values with error bars (± σ(RAP)/$N_{rep}$) at each iteration.](image)

When evaluating performance at the last iteration step, we can see the curves from which the RAP values were generated. Figure 7 presents the performance results for the TST set of %$\%C$ versus SNR for GRLVQI after Stochastic Optimization by Sequential Design (GRLVQI-SD), Baseline GRLVQI using the nominal
settings of [50], and MDA. Notably, GRLVQI outperforms MDA. When GRLVQI settings are optimized via stochastic approximation, classification performance is further improved.

Overall, these performance results are consistent with those of [13]. Although the reference “best” performance values of [13] are included for comparison, direct comparisons with these performance results are not possible since replications were not used in that effort. Thus the work of [13] was essentially “cherry picked” since it involved searching for best of nonreplicated runs. Interestingly, the optimal hyperparameter settings found through Stochastic Approximation are different from those found in [13], indicating the possibility of multiple local optima in ANN solutions.

6. Summary and Conclusions

The cyber attack surface, vectors by which cyber attacks can occur, are increased by sub-internet pathways, e.g. those comprised of common wireless WiFi, Z-Wave, ZigBee and Bluetooth devices. Risks associated with sub-internet pathways include risks of service degradation or disruption which are magnified since e-government pathways include hospitals, power grids and other CI systems. The approach presented herein demonstrates enhancements to sub-internet pathway security with applicable to WPANs.

Herein, a process was presented to find optimal algorithm settings by stochastic approximation which allowed hyperparameter settings to freely change without enforcing bounds as in a design of experiments approach, e.g. [13]. The results illustrate 1) the necessity in determining appropriate GRLVQI algorithm settings, 2) the viability of Stochastic Approximation for RF-DNA Fingerprinting algorithm optimization, and 3) general invariance of conscience learning rates in GRLVQI to accuracy.

Primary contributions include improvements to communication device discrimination using RF Fingerprints by: 1) formalization of a Stochastic

Table 2. Algorithm Optimization Results

<table>
<thead>
<tr>
<th>METHOD</th>
<th>MAXIMIZATION OBJECTIVE</th>
<th>FACTORS LEVELS</th>
<th>PERFORMANCE RESULTS</th>
<th>VERIFICATION AT SNR = 20dB</th>
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<tr>
<td></td>
<td></td>
<td>A</td>
<td>B</td>
<td>C</td>
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<tr>
<td>Stochastic Approximation</td>
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<td>0.016</td>
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<td>Optimization</td>
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<td>Best Full Factorial [13]</td>
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<td>0.05</td>
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<td>N/A</td>
<td>N/A</td>
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Approximation approach for classifier model development, 2) demonstration of this approach for GRLVQI optimization for Z-Wave device discrimination, and 3) improvements in the experimental approach of RF Fingerprinting classifier development by replication.

Results achieved were also similar to those of [13], but comparisons are notional since replications were not considered in [13]. Thus the performance results presented herein are more rigorous by considering both the estimate of the optimal hyper parameter value and the error on that estimate.

Future work includes further refining the sequential design strategy. Firstly, there is no guarantee that the globally optimal point has been found; further work would explore this issue. Secondly, since the algorithm relies on finite differences, we must be reasonably confident in the order relation between estimates of performance at the ±e values of the hyperparameters. This may require increasing the number of training replications per iteration. Thirdly, the sequential design strategy must be adapted to accommodate integer parameters, e.g. the number of PVs.

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8. References